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Sample Calculations – Connection 2

Connection Description

Connection number two consists of a W-section that is welded to an angle on each side of the web, and then bolted to the web of another W-section. There is only one bolt in each angle connection, and the welds runs the full length of all three sides of the angle that are in contact with the W-section. For this connection, we have A992 steel for our two 6 x 12 W-sections and A36 steel for our L 4 x 3 x ¼ angle. A ¾" A325N Hex bolt was used, along with an E-70 electrode weld that was applied using the Shield Metal Arc Welding (SMAW) technique.

Limit States

The limit states that will be looked at for this connection are as follows:

- 1.) Bolt Bearing
- 2.) Bolt Shear Rupture
- 3.) Block Shear
- 4.) Weld Strength

Analysis

The following equations were used to evaluate each limit state

Bolt Bearing:

$$\phi R_n = \min \{ \phi(1.2L_c t F_u); \phi(2.4dt F_u) \}$$

$$\phi = \text{Resistance factor} = 0.75$$

F_u = Ultimate tensile strength of the connected material, in ksi

L_c = Clear distance, in the direction of the force, between the edge of the hole and the edge of the material, in inches

L_e' = effective length from center of bolt hole to rolled edge

L_e = effective length from center of bolt hole to cut edge

t = Thickness of the connected material, in inches

d = Nominal bolt diameter, in inches

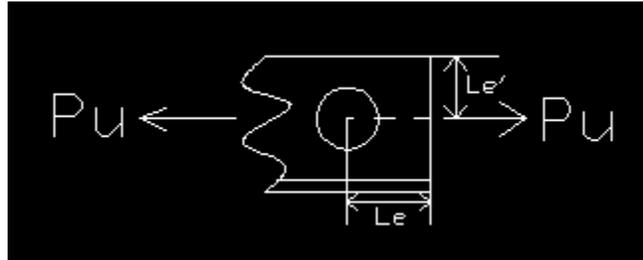
$$R_n = \min \{ [1.2 * (2'' - 0.5 * (0.375'')) * (0.25'') * (58\text{ksi})]$$

$$[2.4 * (0.875'') * (0.25'') * (58\text{ksi})] \}$$

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$$= \min \{64.16 \text{ k}, 30.45 \text{ k}\}$$

$$\text{Therefore, } \phi R_n = (0.75) * (30.45 \text{ k}) = \underline{22.84 \text{ k}}$$



Bolt Shear Rupture:

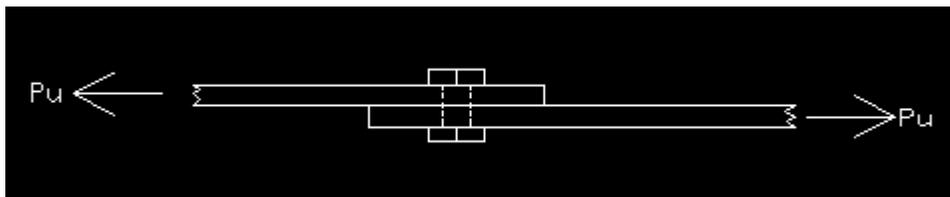
$$\phi R_n = \phi F_n A_b$$

ϕ = Resistance factor = 0.75

F_n = Nominal shear strength F_v tabulated in AISC/LRFD Manual Table J3.2, ksi

A_b = Nominal unthreaded body area of the bolt, in²

$$\phi R_n = (0.75) * (48 \text{ ksi}) * (3/4'')^2 * (\pi/4) = \underline{15.91 \text{ k}}$$



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Block Shear on Angle:

Block shear on W-section will not control because of the two flanges.

$$\phi P_n = \min \{ \phi [(0.6 * F_u) * A_{nv} + U_{bs} * F_u * A_{nt}] \\ \phi [(0.6 * F_y) * A_{gv} + U_{bs} * F_u * A_{nt}] \}$$

ϕ = Resistance factor = 0.75

A_{gv} = Gross area subjected to shear, in²

A_{nv} = Net area subjected to shear, in²

A_{gt} = Gross area subjected to tension, in²

A_{nt} = Net area subjected to tension, in²

U_{bs} = 1.0 since tension stress is uniform

F_y = Minimum yield stress, ksi

F_u = Tensile stress, ksi

$$A_{gv} = 3'' * 0.25'' = 0.75 \text{ in}^2$$

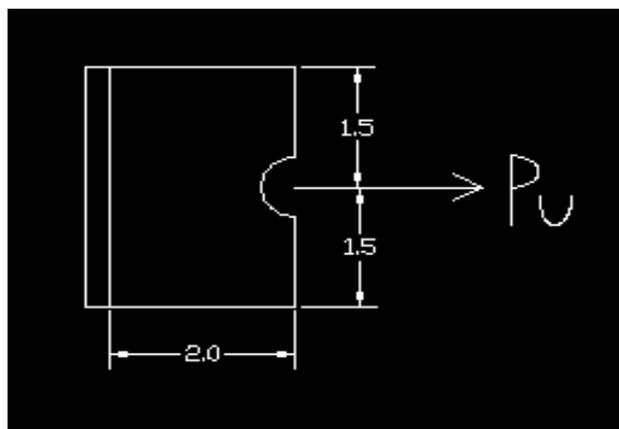
$$A_{nv} = 0.75 \text{ in}^2 - 1 * (1/4'' + 1/16'' + 1/16'') * (1/4'') = 0.656 \text{ in}^2$$

$$A_{gt} = 2'' * 0.25'' = 0.5 \text{ in}^2$$

$$A_{nt} = 0.5 \text{ in}^2 - 0 = 0.5 \text{ in}^2$$

$$\phi P_n = \min \{ [0.75 * (0.6 * 36 \text{ ksi}) * (0.5 \text{ in}^2) + (58 \text{ ksi}) * (0.5 \text{ in}^2)] \\ [0.75 * (0.6 * 58 \text{ ksi}) * (0.656 \text{ in}^2) + (58 \text{ ksi}) * (0.5 \text{ in}^2)] \} \\ = \min \{ 29.85 \text{ k}, 38.87 \text{ k} \}$$

Therefore, $\phi P_n = \underline{29.85 \text{ k}}$



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Weld strength:

$$\phi R_n = \min \{ \phi F_w A_w; \phi F_{bm} A_{bm} \}$$

$$\phi F_w A_w = \phi (0.6 F_{EXX}) * (L_w) * (t_w)$$

$$t_w = 0.707 * D_w$$

$$\phi F_{bm} A_{bm} = \min \{ 0.75 * t_{bm} * L_w * (0.6 F_u);$$

$$0.75 * U * A_n * F_u ;$$

$$1.0 * A_g * (0.6 F_y) \}$$

ϕ = Resistance factor = 0.75

F_{bm} = Nominal strength of the base material, ksi

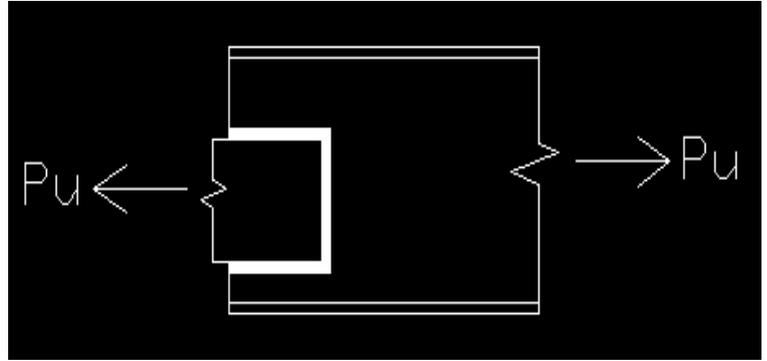
F_y = Tensile yield of base material, ksi

F_{EXX} = Tensile strength of electrode material, ksi

A_w = Effective cross-sectional area of the weld, in²

A_g = Gross cross-sectional area of base material, in²

t_w = Effective throat dimension, in



R_n = Nominal strength of weld design material, kips

F_w = Nominal strength of the weld electrodes

F_u = Tensile strength of base material, ksi

A_{bm} = Cross-sectional area of the base material, in²

A_{nv} = Net area subject to shear, in²

t_{bm} = Thickness of the base material, in

L_w = Length of weld, nominal value, in

$$t_w = 0.707 * 1/4" = 0.177"$$

$$\phi F_w A_w = 0.75 * (0.6 * 70 \text{ ksi}) * 9" * 0.177" = \underline{50.18 \text{ k}}$$

Angle Section

$$\phi F_{bm} A_{bm} = \min \{ 0.75 * 0.25" * 9" * (0.6 * 58 \text{ ksi});$$

$$0.75 * 1.0 * 1.69 \text{ in}^2 * 58 \text{ ksi};$$

$$1.0 * 1.69 \text{ in}^2 * (0.6 * 36 \text{ ksi}) \} = \min \{ 58.73 \text{ k}, 73.52 \text{ k}, 36.50 \text{ k} \}$$

Therefore, $\phi F_{bm} A_{bm}$ (Angle) = 36.50 k

$$\phi F_{bm} A_{bm} = \min \{ 0.75 * 0.230" * 9" * (0.6 * 65 \text{ ksi});$$

$$0.75 * 1.0 * 3.55 \text{ in}^2 * 65 \text{ ksi};$$

$$1.0 * 3.55 \text{ in}^2 * (0.6 * 50 \text{ ksi}) \} = \min \{ 60.55 \text{ k}, 173.06 \text{ k}, 106.50 \text{ k} \}$$

Therefore, $\phi F_{bm} A_{bm}$ (W-section) = 60.55 k

$$\phi R_n = \min \{ 50.18 \text{ k}, 36.50 \text{ k}, 60.55 \text{ k} \} \quad \text{Therefore, } \phi R_n = \underline{36.50 \text{ k}}$$

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CONTROLLING ϕP_N

Once we have all of our values calculated, we need to compare them all to find out which value is the controlling value for our connection.

The final values are:

$$\phi P_n = \min \{22.84 \text{ k}, 15.91 \text{ k}, 29.85 \text{ k}, 36.50 \text{ k}\}$$

$$\phi P_n = 15.91 \text{ k}$$

Therefore, our controlling value for this connection comes from the block shear rupture on the angle bracket.