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Development of correlations for Nusselt number and friction factor for solar air heater with roughened duct having arc-shaped wire as artificial roughness

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11 Abstract

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An experimental study has been carried out for enhancement of heat transfer coefficient of a solar air heater having roughened air duct provided with artificial roughness in the form of arc-shape parallel wire as roughness element. Increment in friction factor by provided with such artificial roughness elements has also been studied. The effect of system parameters such as relative roughness height (e/d)and arc angle $(\alpha/90)$ have been studied on Nusselt number (Nu) and friction factor (f) with Reynolds number (Re) varied from 2000 to 17000. Considerable enhancement in heat transfer coefficient has been achieved with such roughness element. Using experimental data correlations for Nusselt number and friction factor have also been developed for such solar air heaters, which gives a good agreement between predicted values and experimental values of Nusselt number and friction factor.

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20 *Keywords:* Solar energy; Artificial roughness; Nusselt number; Friction factor 21

22 1. Introduction

Solar collectors are being used for thermal conversion to 23 raise the temperature of fluid flowing through the collector. 24 The most commonly used fluids in solar collectors are 25 water and air. Conversion of solar radiations to thermal 26 energy is poor in case of solar air heater mainly due to 27 low heat transfer coefficient between absorber plate and 28 the air flowing in the collector. Close (1963) discussed solar 29 air heaters for low and moderate temperature applications. 30 There are several methods of intentional enhancement of 31 heat transfer. The artificial roughness has been used effec-32 33 tively for enhancing the heat transfer in solar air heaters. In order to attain higher convective heat transfer coefficient 34 it is desirable that the flow at the heat transfer surface 35

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should be turbulent. However, energy for creating turbu-36 lence has to come from the fan or the blower and excessive 37 turbulence means excessive power requirement. It is there-38 fore, desirable that the turbulence must be created only 39 very close to the surface i.e. in laminar sublayer only, where 40 the heat exchange take place and the core of the flow is not 41 unduly disturbed to avoid excessive losses. This can be 42 achieved by using roughened surface on the air side. The 43 heat transfer analogy and friction similarity law for flow 44 in rough pipes having sand grains roughness on the walls 45 of pipes have been developed by Nikuradse (1952). He con- 01 46 ducted an extensive experimental study for turbulent flow 47 of fluids in rough pipes with various degrees of relative 48 roughness height (e/d) and found that the influence of 49 roughness becomes noticeable to a greater degree. The fric-50 tion factor increase with an increase in Reynolds number. 51 The flow particularly characterized by the fact that the 52 resistance factor depends on Reynolds number as well as 53

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Nomenclature

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A	cross-sectional area of the duct, $[A = WH]$, m ²	Nu _{exp}	Nusselt number experimental
$A_{\rm c}$	surface area of collector plate, m ²	Nupre	predicted Nusselt number of rough duct
$C_{\rm d}$	coefficient of discharge for orifice meter	Nus	Nusselt number of smooth duct
$c_{\rm p}$	specific heat of air at constant pressure, kJ/kg K	Ρ	roughness pitch, m
$\overset{r}{D_{\rm h}}, d$	equivalent diameter of the air passage,	Pr	Prandtle number
	$\hat{D}_{\rm h} = 4A/[2(W+H)], {\rm m}$	δρ	pressure drop across the test section of duct, Pa
е	roughness height, m	δp_{o}	pressure drop across the orifice meter, Pa
eld	relative roughness height	q^{-}	rate of heat transfer to air, W/m^2
f	friction factor	Re	Reynolds number
$f_{\rm exp}$	friction factor experimental	$t_{\rm a}$	average temperature of air, K
$f_{\rm pre}$	predicted friction factor for rough duct	t _i	temperature of air at inlet, K
$\dot{f_r}$	friction factor in roughened duct	t _p	average temperature of absorber plate, K
$f_{\rm s}$	friction factor in a smooth passage	t_{o}	temperature of air at outlet, K
H	height of air channel, m	V	velocity of air flow in duct, m/s
h	convective heat transfer coefficient, $W m^{-2} K^{-1}$	W	width of the duct, m
k	thermal conductivity of air, $W m^{-1} K^{-1}$	α	arc angle, degree
L	duct length (test length), m	β	ratio of throat dia of orifice plate and inner dia
т	mass flow rate of air, kg/s		of orifice pipe
Nu	Nusselt number	ho	density of air, kg m^{-3}

on the relative roughness height (e/d). The boundary layer 54 is of the same magnitude as the average roughness height 55 (e/d) and individual projections extend through the bound-56 57 ary layer and cause vortices which produce an additional loss of energy. Therefore, such an enhancement in thermal 58 performance has been found to be accompanied by a sub-59 stantial rise in pumping power required to make the air 60 flow through the collector. The endeavor, therefore, is to 61 provide the roughness geometry in such a way as to keep 62 pressure losses at the lowest possible level while maximum 63 possible gain in heat transfer is obtained. 64

65 The artificially roughened surface can be produced by several methods such as sand grain roughness by sand 66 67 blasting the surface, rib type roughness can be produced by machining, casting, forming, welding, pasting etc. The 68 artificial roughness could be of several shapes such as 69 groove and ridge type or rib type. Dipprey and Sabersky 70 (1963) presented an experimental investigation of the rela-71 tion between heat transfer coefficient and friction factor in 72 73 smooth and rough tubes. Based on the law of wall similarity and the method of Nikuradse (1952); Webb et al. (1971) 74 developed correlations for heat transfer coefficient and fric-75 tion factor for turbulent flow in tubes having a repeated rib 76 77 roughness.

Experimental study has been carried out by Ravigururajan and Bergles (1985) and Sheriff and Gumley (1966) on enhancement of heat transfer coefficient and friction factor for different flow characteristics inside the channels and pipes having artificial roughness over the surface.

Several investigators have investigated for enhancement
of heat transfer in case of solar air heaters using different
geometry and shape of roughness. Prasad and Saini
(1988), Gupta et al. (1991), Malik et al. (1998), Karwa

(1998), Muluwork et al. (1998), Bhagoria et al. (1998), 87 Sahoo and Bhagoria (2005), Thakur et al. (1998), Saini 88 and Saini (1997), Gupta et al. (1993) and Jourker et al. 89 (2006) investigated and developed correlations for Nusselt 90 number and friction factor for different flow conditions in a 91 rectangular duct having roughness elements of different 92 shapes and sizes. Varun et al. (2007) presented a review 93 on roughness geometries used in solar air heaters. There 94 is still scope to identify the suitable roughness element 95 which may be easy to fix on absorber plate. The arc-shape 96 parallel wire of full width length has been used as rough-97 ness element in present study as roughness element, which 98 is easy to fix on absorbing plate. 99

Under the present study an experimental work carried, is 100 based on creating artificial roughness on absorber plate to 101 enhance the heat transfer coefficient between air flowing in 102 the duct and absorber plate. The arc-shape parallel galvan-103 ised iron (GI) wires have been fixed on the under side of 104 absorber plate as artificial roughness. The effect of various 105 parameters such as relative roughness height, relative arc 106 angle have been studied on heat transfer coefficient and fric-107 tion factor with Reynolds number (Re) varied from 2000 and 108 17,000. Relative roughness height (e/d) varied from 0.0213 109 to 0.0422 and relative arc angle ($\alpha/90$) varied from 0.3333 110 to 0.6666. The considerable increase in heat transfer coeffi-111 cient has been achieved. Using experimental data correla-112 tions have been developed for predicting the Nusselt 113 number and friction factor for such solar air heaters. 114

2. Experimental setup

The schematic diagram of test setup is shown in Fig. 1. 116 The setup consists of a duct having artificially roughened 117

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Fig. 1. Schematic diagram of experimental setup.

absorber plate, plenum, heater plate, pipe line, centrifugal
blower and instrumentations for measuring mass flow rate
of air, pressure drop, temperature and voltage for heating
the absorber plate. The various components of experimental setup are discussed below.

123 2.1. Air duct

The most important part of the setup is the duct which
was fabricated from wooden planks having size 2400 mm
long and other dimensions of duct are as shown in Fig.
The aspect ratio has been kept 12 in this study, as many

investigators have established this aspect ratio to be opti-128 mum (Varun et al., 2007). The flow system as shown in 129 Fig. 1 consisted of 900 mm long entry section, 1000 mm 130 long test section and 500 mm long exit section. The entry 131 and exit length of the flow have been kept to minimize 132 the end effects on the test section considering the recom-133 mendations provided in ASHRAE (1977). The bottom 134 plate was made of 28 mm thick wooden plank provided 135 with 1 mm thick mica laminate and 6 mm thick wooden 136 ply on top of wooden plank to have a smooth surface as 137 shown in Fig. 3. The sidewalls of duct were also made of 138 40 mm thick wooden plank having smooth surface. 139



Fig. 2. Sectional view of duct.

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Fig. 4. Heater plate along with details of heating element.

140 2.2. Heater plate

The heater plate consisted of a 6 mm thick asbestos 141 142 sheet, mica, nichrome wire, wooden ply, and glass wool. The details of the heater plate are shown in Fig. 4. The hea-143 144 ter plate was 1500 mm long and 300 mm wide, having 5 loops of nichrome wire connected by combining series 145 and parallel loops. The wires were fixed on asbestos sheet 146 covered with strips of mica to keep the uniform distance 147 148 between the wires. The heater was fabricated to produce about 1000 W/m^2 heat energy in the form of radiations 149 which was considered equivalent to a standard value of 150 solar radiation as in case of solar air heaters. Each wire 151 loop having equivalent resistance of 60Ω was connected 152 153 in parallel to have a total resistance of 12 Ω . With the help of a variac (voltage regulator) a voltage of 80 V across the 154 wire loops having total resistance of 12Ω was maintained. 155 Corresponding to this voltage of 80 V and resistance of 156 12Ω about 530 W energy over a surface area of 0.45 m² 157

 $(1500 \text{ mm} \times 450 \text{ mm})$ was obtained. This heat energy was
considered to be sufficient to produce about 1000 W/m^2 158heat energy in the form of radiation. An asbestos sheet
has been fixed on 76 mm deep wooden box, made of
12 mm thick wooden ply, filled with glass wool as insulat-
ing material on the top of heater plate to minimize the heat
losses.160

2.3. Absorber plate 165

The absorber plate is made up of 0.5 mm thick GI sheet. 166 The arc-shape wires are pasted on the backside of the GI 167 sheet as shown in Fig. 5. The orientation of wires in the 168 form of parallel arc as shown in Fig. 6 are provided as arti-169 ficial roughness on the absorber plate. The diameter of wire 170 has been varied to get different heights of roughness. The 171 radius of arc has also been varied to get different angles 172 of attack, however the relative pitch (P/e) has been kept 173 constant. 174





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Fig. 6. Details of wire contour.

175 **3. Instrumentation**

176 The mass flow rate of air through the duct was measured by using a calibrated orifice meter and inclined manometer. 177 The orifice plate is fitted between two flanged pipes of suit-178 able length to keep the orifice plate concentric with the 179 pipe. The pressure drop across the test section has been 180 measured by a micro manometer having 0.01 mm accuracy. 181 The butyl alcohol having density of 800 kg/m³ has been 182 used in manometer to increase the accuracy further. 183

The temperatures at various locations were measured 184 with the calibrated 0.3 mm dia Copper constantan thermo-185 couples along with digital micro voltmeter to indicate the 186 output in K with an accuracy of 0.1 K. Thermocouples 187 have been used on the top surface of absorber plate to 188 record the temperature of plate, the positions of these ther-189 mocouples are shown in Fig. 7. The temperature of air 190 191 inside the duct has been recorded by thermocouples. The positions of these thermocouples and air taps are as shown 192 in Fig. 8. 193

4. Range of parameter

The present experimental study have been conducted for the following parameters:

		209
Reynolds number (Re)	2000-17 000	200
Relative angle of attack ($\alpha/90$)	0.3333-0.6666	204
Relative roughness height (e/d)	0.0213-0.0422	202
Relative pitch (P/e)	10	200
Duct aspect ratio (W/H)	12	198

5. Experimental procedure

The experimental data have been generated as per the recommendations of ASHRAE (1977) for testing of solar collectors operating in open loop flow mode. A duct is being assembled as shown in Fig. 3, having all smooth surfaces including absorber plate was used to collect the data for verification of test setup. The smooth absorber plate is 216



Fig. 7. Location of thermocouples on absorber plate.



Fig. 8. Location of thermocouples and air taps in the air duct.

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Fig. 9. Comparison of experimental and predicted values from modified Blasius equation of friction factor vs. Reynolds number.

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than replaced with the rough plate having the arc-shape 217 wires fixed on the under side of the plate. All joints of duct, 218 219 inlet section, test section, exit section, plenum and pipes are thoroughly checked up for any leakage before starting the 220 experiment every time. All the measuring equipments were 221 checked up before starting the experiment. The flow rate of 222 air in the duct has been maintained for about 30 min, 223 224 assuming the steady state condition established for each flow rate. Ten different flow rates were used for each absor-225 ber plate having different roughness parameter. Following 226 parameters were measured for each set of readings: 227

(i) Pressure drop across the test section of duct.

- (ii) Pressure across the orifice plate to measure the air flow rates.
- 231 (iii) Temperature of absorber plate.
 - (iv) Temperature of air inside the duct.
 - (v) Ambient temperature.

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234 (vi) Voltage supplied to heater plate.

In order to verify the validity of the experimental setup
the values of Nusselt number and friction factor were compared with the values obtained from correlations available
in the literature for smooth duct namely Dittus–Boelter
equation (Han et al., 1985) and modified Blasius equation
(Han et al., 1985).

242 6. Equations used for calculation

 $m = Cd \left[\frac{2\rho(\delta p_0)}{(1-\beta^4)} \right]^{0.5}$

The following equations were used for calculating the mass flow rate of air, m (Saini and Saini, 1997), heat energy transfer, q, heat transfer coefficient, h (Saini and Saini, 1997)

$$u = mc_p(t_o - t_i) \tag{2}$$

$$=\frac{q}{A_{\rm c}(t_{\rm p}-t_{\rm a})}\tag{3}$$

where t_p and t_a are average values of absorber plate tem-251 perature and air temperature, respectively. The average 252 temperature of the plate was determined from the temper-253 ature recorded at fifteen different locations along the test 254 section of the absorber plate as shown in Fig. 7. It was 255 found that the temperature of the absorber plate varies pre-256 dominantly in the flow direction only and is linear. The 257 variations in temperature in the direction normal to the 258 flow direction were found to be negligible. The air temper-259 ature variations were found to be linear since the tempera-260 ture variations of the absorber plate in the direction normal 261 to the flow were found to be negligible in that direction, the 262 air temperature variations in that direction can be assumed 263 to be negligible the temperature variation in the direction 264 normal to the absorber plate could not be measured 265 because of very small duct depth and were assumed to be 266 negligible. The air temperature was determine as an aver-267 age of the temperatures measured at six central locations 268 over the test length of the duct along the flow direction 269 as shown in Fig. 8. 270

The Nusselt number was calculated by using the following equation: 271

$$Nu = \frac{hD_{\rm h}}{k} \tag{4}$$

The values of pressure drop were measured across the275test section by micro manometer and these values were276used for determining the friction factor using following277equation:278

(1)
$$f = \frac{2\delta p D_{\rm h}}{4\rho L V^2} \tag{5}$$

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Fig. 10. Comparison of experimental and predicted values from modified Dittus-Boelter equation of Nusselt number vs. Reynolds number.

As mentioned earlier, the experiments were carried out 281 for a smooth duct to verify the validity. The values of fric-282 tion factor and Nusselt number obtained from the experi-283 284 ments were compared with the values obtained from 285 correlations of the Dittus-Boelter equation (Han et al., 1985) for the Nusselt number and modified Blasius equa-286 tion for the friction factor. The modified Blasius equation 287 (Han et al., 1985) was used as given below 288

290
$$f_s = 0.85 Re^{-0.25}$$
 (6)

The Nusselt number for a smooth rectangular duct is given by the Dittus and Boelter (Han et al., 1985) equation given below

295
$$Nu_s = 0.024 Re^{0.8} Pr^{0.4}$$
 (7)

The deviation in the present experimental friction data collected for smooth duct used in experiments as compared to the values predicted by modified Blasius equation are shown in Fig. 9. The deviation of Nusselt number data from the value predicted from Dittus–Boelter equation (Han et al., 1985), and the experimental values duct are shown in Fig. 10. The experimental values of the friction302factor and Nusselt number establishes the accuracy of the303experimental data collected with the present experimental304setup.305

7. Results and discussions

Figs. 11-14 have been drawn to represent the Nusselt 307 number and friction factor derived from the test results 308 as a function of the system and operating parameters. It 309 can be seen from the figures that for given values of rough-310 ness parameters, the Nusselt number increases monoto-311 nously with increasing Reynolds number, where as the 312 friction factor decreases as the Reynolds number increases. 313 It can also be seen that enhancement in Nusselt number 314 also increases with an increase of Reynolds number. 315

Fig. 11 shows the variation in Nusselt number with Reynolds number for different values of relative roughness (e/ 317 d) from 0.0213 to 0.0422. It is seen from the figure that considerable enhancement is achieved in heat transfer coefficient by providing the arc-shape roughness element. It is 320



Fig. 11. Variation of Nusselt number with Reynolds number for different values of e/d.

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Fig. 12. Variation of friction factor with Reynolds number for different values of e/d.



Fig. 13. Variation of Nusselt number with Reynolds number for different values of $\alpha/90$.





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also seen that Nusselt number increases with an increase in relative roughness and is maximum corresponding to relative roughness (e/d) of 0.0422. Fig. 12 shows the effect of relative roughness height (e/d) on friction factor. It is observed that friction factor also increase with an increase in relative roughness height (e/d) and for a given value of arc angle ($\alpha/90$).

The effect of relative angle of attack ($\alpha/90$) on Nusselt number and friction factor has been shown in Figs. 13 and 14.

Fig. 13 shows the effect of relative angle of attack ($\alpha/90$) 331 on Nusselt number from 0.3333 to 0.6666. It is seen that for 332 a given value of e/d the value of Nusselt number decrease 333 with the increase of relative arc angle ($\alpha/90$). It could be 334 explained on the similar lines of the study conducted by 335 Prasad and Saini (1988) for transverse wires. The angle 336 of attack for the arc-shape geometry becomes towards 337 transverse direction for small value of arc angle (α / 338 90 = 0.3333) which results in maximum heat transfer coef-339 ficient. However, the trend in friction factor has been found 340 reversed. The friction factor has been observed maximum 341 342 for maximum value of relative arc angle ($\alpha/90$). This could 343 be the advantage of such geometry of artificial roughness with solar air heaters. 344

The maximum enhancement obtained in Nusselt num-345 ber is 3.80 times with a maximum increase in friction factor 346 at 1.75 times. Further it has been observed from the Figs. 347 11-14 that enhancement in heat transfer and increase in 348 friction factor is negligible for the Reynolds number less 349 than 4000. Using roughened absorber plate with solar air 350 heater may not be advantageous in this range of Reynolds 351 number. 352

353 8. Development of correlations for Nusselt number and354 friction factor

In order to make useful such study by designer and researcher it becomes necessary to develop the correlations for heat transfer coefficient and friction factor having various parameters investigated. Accordingly, using experimental data correlations for Nusselt number and friction factor have been developed and discussed as follows.

8.1. Correlation for Nusselt number

Based on the experimental study, the effect of various parameters on Nusselt number have been discussed earlier and are reproduced as follows:

- i. Nusselt number increases monotonically with increasing Reynolds number (*Re*).
- ii. Nusselt number increases with increase in relative roughness height of roughness (e/d).
- iii. Nusselt number decrease with the increase in relative angle of arc ($\alpha/90$) and maximum value is observed at relative arc angle of 0.3333.

The Nusselt number is strongly dependent on roughness parameters, e/d, $\alpha/90$ and the operating parameter *Re*. Thus the equation for Nusselt number can be written as

$$Nu = f(Re, e/d, \alpha/90)$$
 (8) 377

The data collected from the experimental study for temperature of air and plate, manometer reading across the orifice for calculating air mass flow rate to calculate the heat transfer coefficient. The Nusselt number calculated by using the heat transfer coefficient were plotted against Reynolds number and are shown in Fig. 15. The regression analysis has been carried out to fit a straight line through the data point, the regression resulted the following:

$$Nu = C_0 R e^{1.3186} (9) 387$$

The constant C_0 is dependent of the parameters e/d and $\alpha/90$. The relative roughness height (e/d) is incorporated to show the effect of roughness height on Nusselt number. The values of $Nu/Re^{1.3186}$ are plotted against relative roughness height (e/d) as shown in Fig. 16.

Now, regression analysis was carried out to fit a straight 393 line through these points, and prepared as follows: 394

$$Nu = C_1 R e^{1.3186} (e/d)^{0.3772}$$
(10) 396

The constant C_1 is the function of remaining parameter, 397 of relative arc angle ($\alpha/90$). To include the effect of $\alpha/90$, 398 this parameter is incorporated and the values of *Nul* 399





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Fig. 16. Plot of *Nu/Re*^{1.3186} vs. *e/d*.

400 $(Re^{1.3186}(e/d)^{0.3772})$ are plotted against the values of $\alpha/90$, as 401 shown in Fig. 17. The best fit regression yields the follow-402 ing correlation for Nusselt number:

404
$$Nu = 0.001047Re^{1.3186}(e/d)^{0.3772}(\alpha/90)^{-0.1198}$$
 (11)

The calculated values of Nusselt number from developed correlation have been compared with the experimental values as shown in Fig. 18. It has been found that these values are reasonably good as maximum deviation found within $\pm 10\%$.

410 8.2. Correlation for friction factor

As discussed earlier under results and discussions the
effect of various parameters on friction factor are reproduced as

- 414 i. Friction factor decreases with increasing Reynolds415 number (*Re*).
- 416 ii. Friction factor increases with increase in relative 417 roughness height (e/d).
- 418 iii. The values of friction factor increase with relative arc419 angle.

The friction factor dependents strongly on roughness 421 parameters, e/d, $\alpha/90$ and the operating parameter, *Re.* 422 Thus the equation for friction factor can be written as 423

$$f = f(Re, e/d, \alpha/90)$$
 (12) 425

By following similar procedure of correlation for Nusselt number the regression analysis has been carried out to fit a straight line through the data point for friction factor shown in Fig. 19. The relationship is as follows: 429

$$f = C_2 R e^{-0.17103} \tag{13}$$

The constant C_2 is dependent of the parameters e/d and 432 $\alpha/90$. The relative roughness height e/d introduced to incorporate the effect of roughness height on friction factor. The values of $Nu/\text{Re}^{-0.17103}$ are plotted against relative height of 435 wire (e/d) as shown in Fig. 20. The regression analysis was carried out to fit a straight line through these points, and reproduced by following expression: 438

$$f = C_3 R e^{-0.17103} (e/d)^{0.1765}$$
(14) 440

The constant C_3 is a function of other remaining parameter, relative arc angle ($\alpha/90$). This parameter is incorporated and the values of $f/Re^{-0.17103}(e/d)^{0.1765}$ are plotted 443



Fig. 17. Plot of $Nu/(Re^{1.3186}(e/d)^{0.3772})$ vs. $\alpha/90$.





Fig. 18. Comparison of predicted and experimental values of Nusselt number.



Fig. 19. Friction factor vs. Reynolds number.



Fig. 20. Plot of $f/Re^{-0.1710}$ vs. e/d.

444 against the values of $\alpha/90$, as shown in Fig. 21. The final 445 form of the correlation for friction factor is obtained as 446 follows:

448
$$f = 0.14408Re^{-0.17103}(e/d)^{0.1765}(\alpha/90)^{0.1185}$$
 (15)

The values of friction factor calculated by using the correlation are compared with the experimental values as shown in Fig. 22. It is seen from the Fig. 22 that the developed correlation for friction factor, can predict the values of friction factor reasonably correct in the range of param-453

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Fig. 22. Comparison of predicted and experimental values of friction factor.

eters studied. The maximum deviation for these cases has been found to be $\pm 10\%$.

456 9. Conclusions

It has been concluded that considerable enhancement in 457 heat transfer coefficient is achieved by providing arc-shape 458 parallel wire geometry as artificial roughness with solar air 459 duct. The maximum enhancement in Nusselt number has 460 been obtained as 3.80 times corresponding the relative 461 arc angle ($\alpha/90$) of 0.3333 at relative roughness height of 462 0.0422. However, the increment in friction factor corre-463 sponding to these parameters has been observed 1.75 times 464 465 only.

Based on the experimental values, correlations for Nusselt number and friction factor have been developed. The
good agreement has been found between calculated and
experimental values.

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